

$$1a \quad f(x) = 1 - x^2$$

$$\lim_{h \rightarrow 0} \frac{(1 - (x+h)^2) - (1 - x^2)}{x+h-x} = \frac{1 - (x^2 + 2xh + h^2) - 1 + x^2}{h}$$

$$\lim_{h \rightarrow 0} = \frac{\cancel{1} - \cancel{x^2} - 2xh + h^2 - \cancel{1} + \cancel{x^2}}{h} = \frac{-2xh + h^2}{h} = -2x + h = \boxed{-2x}$$

$$\text{at } x=2 \quad -2(2) = -4$$

$$1b \quad \lim_{h \rightarrow 0} \frac{(2(x+h)^2 + 5(x+h)) - (2x^2 + 5x)}{x+h-x} = \frac{\cancel{2x^2} + 4xh + 2h^2 + \cancel{5x} + 5h - \cancel{2x^2} - \cancel{5x}}{h}$$

$$\frac{4xh + 2h^2 + 5h}{h} = 4x + 2h + 5 = \boxed{4x+5}$$

$$\text{at } x=-1 \quad 4(-1) + 5 = 1$$

$$1c \quad \lim_{h \rightarrow 0} \frac{(5 - 2(x+h)^2) - (5 - 2x^2)}{x+h-x} = \frac{\cancel{5} - \cancel{2x^2} - 4xh - 2h^2 - \cancel{5} + \cancel{2x^2}}{h}$$

$$\lim_{h \rightarrow 0} \frac{-4xh - 2h^2}{h} = -4x - 2h = \boxed{-4x}$$

$$\text{at } x=3 \quad -4(3) = -12$$

$$1d \quad \lim_{h \rightarrow 0} \frac{3(x+h) + 5 - (3x+5)}{x+h-x} = \frac{\cancel{3x} + 3h + \cancel{5} - \cancel{3x} - \cancel{5}}{h}$$

$$\frac{3h}{h} = \boxed{3} \rightarrow \text{the slope at any point is always } 3$$

$$2a \quad \lim_{h \rightarrow 0} \frac{\frac{4}{x+h} - \frac{4}{x}}{x+h-x} = \frac{\frac{4x - 4(x+h)}{x(x+h)}}{h} = \frac{-4h}{\frac{x(x+h)}{h}} = \frac{-4}{x(x+h)}$$

$$\lim_{h \rightarrow 0} \frac{-4}{x(x+h)} = \frac{-4}{x^2}$$